

Carmel Convent School  
UNIT TEST MAY 2023  
CLASS X (MATHEMATICS)

TIME 1 hr 30 min

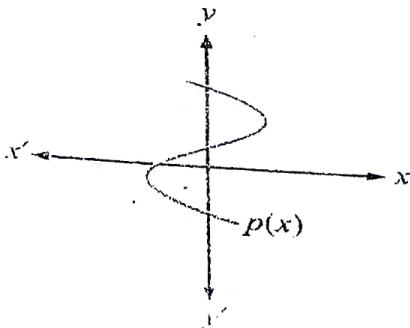
MM 40

General Instructions

1. All questions are compulsory
2. SECTION A Q1 to Q8 1 mark each ( MCQ)
3. SECTION B Q 9 to Q 11 2 marks each
4. SECTION C Q 12 to Q 15 3 marks each
5. SECTION D Q 16 & 17 5 marks each
6. SECTION E Q 18 4 Marks( 1+1+2 ) Case Study

SECTION A

- Q1 If  $p$  and  $q$  are two consecutive natural numbers, then HCF of  $(p, q)$  is  
a)  $q$     b)  $p$     c)  $1$     d)  $pq$
- Q2 The decimal expansion of the rational number  $31 \div (2^2 \times 5)$  will terminate after  
a) one decimal place    b) two decimal places  
c) 3 decimal places    d) more than 3 decimal places
- Q3 In the given figure, the graph of polynomial  $p(x)$  is shown. The number of zeros of  $p(x)$  is



- a) 3    b) 4    c) 1    d) 2

Q4 If 1 is the zero of polynomial  $P(x) = ax^2 - 3(a-1)x - 1$ , then the value of a is  
 a) -1    b) 1    c) -2    d) 2

Q5 The value of k for which the pair of linear equations  
 $4x + 6y - 1 = 0$                        $2x + ky - 7 = 0$   
 represent parallel lines is  
 a) 3    b) -2    c) -2    d) 4

Q6 In this question, a statement of assertion(A) is followed by a statement of reason(R). Choose the correct option :  
 a) Both assertion(A) and reason (R) are true and reason(R) is the correct explanation of assertion (A)  
 b) Both assertion(A) and reason (R) are true and reason(R) is not the correct explanation of assertion(A)  
 c) Assertion(A) is true but reason (R) is false  
 d) Assertion(A) is false but reason (R) is true

Assertion(A) : The area of trapezium formed by the lines  
 $3x + 4y - 12 = 0$  and  $3x + 4y = 6$  is  $9/2$  square units.

Reason (R) : The system of equations  $a_1x + b_1y + c_1 = 0$  and  
 $a_2x + b_2y + c_2 = 0$  is inconsistent, if  $a_1/a_2 = b_1/b_2 = c_1/c_2$

Q7 Which of the following is not defined?  
 a)  $\sin 90^\circ$     b)  $\tan 0^\circ$   
 c)  $\cot 90^\circ$     d)  $\operatorname{cosec} 0^\circ$

	0	$30^\circ$	$45^\circ$	$60^\circ$	$90^\circ$
sin	0	$1/2$	$1/\sqrt{2}$	$\sqrt{3}/2$	1
cos	1	$\sqrt{3}/2$	$1/\sqrt{2}$	$1/2$	0
tan	0	$1/\sqrt{3}$	1	$\sqrt{3}$	N.D.

Q8 If  $\sin \theta = 1/2$  then find the value of  $\sin \theta (\sin \theta - \operatorname{cosec} \theta)$   
 a)  $3/4$     b)  $-3/4$     c)  $\sqrt{3}/2$     d)  $-\sqrt{3}/2$

### SECTION B

Q9 A merchant has 120 L of oil of one kind, 180 L of another kind and 240 L of the third kind. He wants to sell the oil by filling the three kinds of oil in the tins of equal capacity. What should be the greatest capacity of such a tin?

Q10 Find a quadratic polynomial, the sum and product of whose zeros are  $\sqrt{2}$  and  $-3/2$  respectively.

Q11 Given that  $\sin \alpha = 1/2$  and  $\cos \beta = \sqrt{3}/2$ . Then find the value of  $\alpha + \beta$

### SECTION C

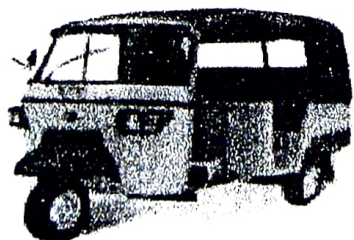
- ~~Q12~~ Prove that  $3 + \sqrt{2}$  is an irrational number.
- ~~Q13~~ Find the zeros of the following quadratic polynomial and verify the relationship between the zeros in the coefficient.  
 $3x^2 - x - 4$
- ~~Q14~~ Solve  $x + y = 3$  and  $2x + 5y - 12 = 0$  and hence find the value of  $m$  for which  $y = mx + 5$ .
- ~~Q15~~ If  $\operatorname{cosec} A = 2$ , then find the value of  $(\cot A + \sin A) / (1 + \cos A)$

### SECTION D

- ~~Q16~~ Solve the following pair of linear equations in two variables.  
 $3x + y - 11 = 0$   
 $x - y + 1 = 0$   
Shade the region bounded by these lines along X axis and Y axis. Also find the area of the region bounded by the lines at both X axis and Y axis.
- ~~Q17~~ (i) Find the value of  
 $(1 + \tan \theta + \sec \theta) (1 + \cot \theta - \operatorname{cosec} \theta)$
- (ii) Prove the following identity  
 $(\operatorname{cosec} \theta - \cot \theta)^2 = (1 - \cos \theta) / (1 + \cos \theta)$

### SECTION E ( Case Study)

- ~~Q18~~ It is common that Governments revise travel fares from time to time based on various factors such as inflation ( a general increase in prices and fall in the purchasing value of money) on different types of vehicles like auto, Rickshaws, taxis, Radio cab etc. The auto charges in a city comprise a fixed charge together with the charge for the distance covered. Study the following situations:



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