



# DELHI PUBLIC SCHOOL, CHANDIGARH

Periodic Test - 2, Session 2024-25

Class: X Subject: Maths (Set 1)

MM: 80

Time: 3:00 hrs Aashita

## General Instructions:

1. This Question paper contains - five sections A, B, C, D and E. Each section is compulsory. However, there are internal choices in some questions.
2. Section A has 18 MCQ's and 02 Assertion-Reason based questions of 1 mark each.
3. Section B has 5 Very Short Answer (VSA)-type questions of 2 marks each.
4. Section C has 6 Short Answer (SA)-type questions of 3 marks each.
5. Section D has 4 Long Answer (LA)-type questions of 5 marks each.
6. Section E has 3 source based/case based / passage based/integrated units of assessment (4 marks each) with sub parts.
7. All Questions are compulsory. However, an internal choice in 2 Questions of 5 marks, 2 Questions of 3 marks and 2 Questions of 2 marks has been provided.

## Section - A

1. The values of  $x$  and  $y$  in the given figure are:



a)  $x = 10, y = 14$

e)  $x = 21, y = 84$

b)  $x = 21, y = 25$

d)  $x = 10, y = 40$

2. If two positive integers  $a$  and  $b$  are written as  $a = p^3q^4r^6$  and  $b = p^6q^2r^4$ , where  $p, q, r$  are prime numbers, then the result obtained by dividing the product of the positive integers by the LCM ( $a, b$ ) is:

a)  $p^3q^4r^4$

e)  $p^3q^2r^4$

b)  $p^3q^4r^2$

d)  $p^6q^4r^6$

3. The greatest number which divides 87 and 97 leaving 7 as remainder is

a) 10

c)  $87 \times 97$

b) 1

d) 6300

4. If one zero of the polynomial  $p(x) = x^2 - 3kx + 4k$  be twice the other, then the value of  $k$  is:

a) -2

e) 2

b)  $\frac{1}{2}$

d)  $-\frac{1}{2}$

5. If  $\alpha, \beta$  are the zeroes of the polynomial  $x^2 - 1$ , then the value of  $(\alpha + \beta)$  is:

a) -1

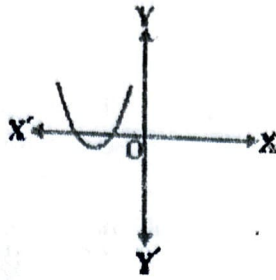
c) 1

b) 0

d) 2

6. The number of zeroes of  $p(x)$  in the given figure is:

- a) one  
b) two  
c) three  
d) four



7. The pair of equations  $y = 0$  and  $y = -7$  has:

- a) one solution  
b) infinitely many solutions  
c) two solutions  
d) no solution

8. 3 chairs and 1 table cost ₹ 900, whereas 5 chairs and 3 tables cost ₹ 2100. If the cost of 1 chair is ₹  $x$  and the cost of 1 table is ₹  $y$ , then the situation can be represented algebraically as

- a)  $3x + y = 900, 3x + 5y = 2100$   
b)  $x + 3y = 900, 3x + 5y = 2100$   
c)  $3x + y = 900, 5x + 3y = 2100$   
d)  $x + 3y = 900, 5x + 3y = 2100$

9. The ratio of the sum and product of the roots of the equation  $7x^2 - 12x + 18$  is:

- a) 7 : 12  
b) 3 : 2  
c) 7 : 18  
d) 2 : 3

10. If the quadratic equation  $ax^2 + bx + c = 0$  has two real and equal roots, then the value of 'c' is:

- a)  $\frac{-b}{2a}$   
b)  $\frac{b}{2a}$   
c)  $\frac{-b^2}{4a}$   
d)  $\frac{b^2}{4a}$

11. If  $p - 1, p + 1$  and  $2p + 3$  are in A.P., then the value of  $p$  is:

- a) 0  
b) 2  
c) -2  
d) 4

12.  $\frac{\cos^2\theta}{\sin^2\theta} - \frac{1}{\sin^2\theta}$  in simplified form is

- a)  $\sec^2\theta$   
b) 1  
c)  $\tan^2\theta$   
d) -1

13. The common difference of the A.P. whose  $n$ th term is given by  $a_n = 3n + 7$ , is:

- a) 7  
b)  $3n$   
c) 3  
d) 1



### Section - B

21. For what values of  $k$  does the pair of equations given below have a unique solution?

$$6x + ky + 9 = 0$$

$$2x + 3y + 4 = 0$$

OR

Solve the following pair of linear equations by elimination method:

$$7x - 2y = 3$$

$$11x - \frac{3}{2}y = 8$$

22. A bag contains 4 red, 3 blue and 2 yellow balls. One ball is drawn at random from the bag. Find the probability that ball drawn is

a) red  $\frac{4}{9}$

b) yellow  $\frac{2}{9}$

23. ✓ If  $4 \cot^2 45^\circ - \sec^2 60^\circ + \sin^2 60^\circ + p = \frac{3}{4}$ , then find the value of  $p$ . 0

OR

If  $\cos A + \cos^2 A = 1$ , then find the value of  $\sin^2 A + \sin^4 A$ .

24. A survey conducted on 20 households in a locality by a group of students resulted in the following frequency table for the number of family members in a household:

| Family Size     | 1 - 3 | 3 - 5 | 5 - 7 | 7 - 9 | 9 - 11 |
|-----------------|-------|-------|-------|-------|--------|
| No. of families | 7     | 8     | 2     | 2     | 1      |

Find the mode. 3.4

25. Find the discriminant of the quadratic equation  $2x^2 - 4x + 3 = 0$  and hence find the nature of its roots. -8, not real

### Section - C

26. Prove that  $2 + \sqrt{5}$  is an irrational number. ✓
27. Find the zeroes of the quadratic polynomial  $x^2 - 3$  and verify the relationship between the zeroes and the coefficients.  $-\sqrt{3}, \sqrt{3}$
28. Determine the AP whose third term is 16 and 7<sup>th</sup> term exceeds the 5<sup>th</sup> term by 12.

OR

- ✓ How many terms of the AP: 24, 21, 18, 15, ..... must be taken so that their sum is 78? 4
29. From the top of a 7m high building, the angle of elevation of the top of a cable tower is  $60^\circ$  and the angle of depression of its foot is  $45^\circ$ . Determine the height of the tower. 7 (1+ $\sqrt{3}$ )m.

30. If  $\sec \theta = \frac{13}{12}$ , then find  $\sin \theta$  and  $\cot \theta$ .

OR

Prove that  $\sec A (1 - \sin A)(\sec A + \tan A) = 1$

31. One card is drawn from a well shuffled deck of 52 cards. Find the probability of getting

- a) a red face card  $\frac{6}{52}$
- b) The queen of diamonds  $\frac{1}{52}$
- c) a spade  $\frac{13}{52}$

### Section - D

32. A train travels at a certain average speed for a distance of 54km and then travels a distance of 63km at an average speed of 6km/hr more than the first speed. If it takes 3 hours to complete the journey, what was its first average speed?  $36 \text{ km/hr}$

33. A lending library has a fixed charge for the first three days and an additional charge for each day thereafter. Anu paid ₹27 for a book kept for seven days, while Neeru paid ₹ 21 for the book she kept for five days. Find the fixed charge and the charge for each extra day.  $15, 3$

34. Prove that  $\frac{\cos \theta - \sin \theta + 1}{\cos \theta + \sin \theta - 1} = \operatorname{cosec} \theta + \cot \theta$

OR

Prove that  $\frac{\tan A}{1 - \cot A} + \frac{\cot A}{1 - \tan A} = 1 + \sec A \cdot \operatorname{cosec} A$

35. The following distribution shows the daily pocket allowance of children of a locality. The mean pocket allowance is ₹18. Find the missing frequency  $f$ .  $\rightarrow 20$

| Daily pocket allowance (in ₹) | 11 - 13 | 13 - 15 | 15 - 17 | 17 - 19 | 19 - 21 | 21 - 23 | 23 - 25 |
|-------------------------------|---------|---------|---------|---------|---------|---------|---------|
| No. of children               | 7       | 6       | 9       | 13      | f       | 5       | 4       |
|                               | 10      | 9       | 12      | 16      | 13      | 8       | 7       |

OR

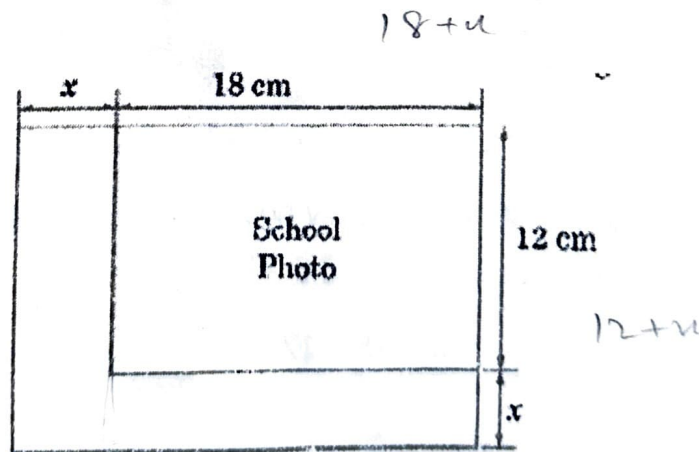
The median of the following data is 525. Find the missing frequencies  $x$  and  $y$ , if the total of the frequencies is 100.

| Class Intervals | Frequency |
|-----------------|-----------|
| 0 – 100         | 2         |
| 100 – 200       | 5         |
| 200 – 300       | x         |
| 300 – 400       | 12        |
| 400 – 500       | 17        |
| 500 – 600       | 20        |
| 600 – 700       | y         |
| 700 – 800       | 9         |
| 800 – 900       | 7         |
| 900 – 1000      | 4         |

### Section – E

36. **Case Study 1:** While designing the school year book, a teacher asked the student that the length and width of a particular photo is increased by  $x$  units each to double the area of the photo. The original photo is 18cm long and 12cm wide.

Based on the above information, answer the following questions:



- Write an algebraic equation depicting the above information.  $x^2 + 30x - 216$  (1)
- Write the corresponding quadratic equation in standard form.  $x^2 + 30x - 216$  (1)
- What should be the new dimensions of the enlarged photo? 24, 18.

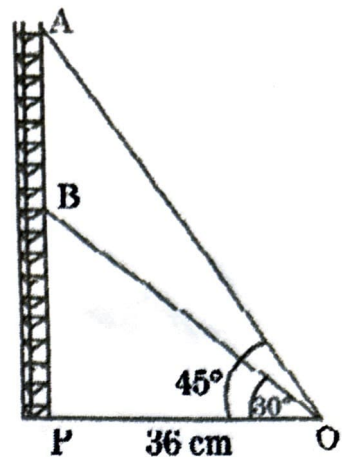
OR

Can any rational value  $x$  make the new area equal to 220 cm<sup>2</sup>? (2)

37.

**Case Study 2:** Radio towers are used for transmitting a range of communication services including radio and television. The tower will either act as an antenna itself or support one or more antennas on its structure. On a similar concept, a radio station tower was built in two Sections A and B. Tower is supported by wires from a point O.

Distance between the base of the tower and the point O is 36cm. From point O, the angle of elevation of the top of the Section B is  $30^\circ$  and the angle of elevation of the top of Section A is  $45^\circ$ .



Based on the above information, answer the following questions:

- i) Find the length of the wire from the point O to the top of Section B.  $24\sqrt{3}$  (1)
- ii) Find the height of the Section A from the base of the tower. 36 (1)
- iii) Find the distance AB.  $12(3-\sqrt{3})$

**OR**

Find the area of  $\Delta OPB$ .

(2)

38.

**Case Study 3:** In the month of April to June 2022, the exports of passenger cars from India increased by 26% in the corresponding quarter of 2021-22, as per a report. A car manufacturing company planned to produce 1800 cars in 4<sup>th</sup> year and 2600 cars in 8<sup>th</sup> year. Assuming that the production increase uniformly by a fixed number every year.



Based on the above information, answer the following questions:

- i) Find the production in the 1<sup>st</sup> year. 1200 (1)
- ii) Find the production in the 12<sup>th</sup> year. 3400 (1)
- iii) Find the total production in first 10 years. 21,000

**OR**

In how many years will the total production reach 31200 cars? (2)